

Elastomeric silicone substrates for terahertz fishnet metamaterials

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In this work, we characterize the electromagnetic properties of polydimethylsiloxane (PDMS) and use this as a free-standing substrate for the realization of flexible fishnet metamaterials at terahertz frequencies. Across the 0.2–2.5 THz band, the refractive index and absorption coefficient of PDMS are estimated as 1.55 and $0\text{--}22\text{ cm}^{-1}$, respectively. Electromagnetic modeling, multi-layer flexible electronics microfabrication, and terahertz time-domain spectroscopy are used in the design, fabrication, and characterization of the metamaterials, respectively. The properties of PDMS add a degree of freedom to terahertz metamaterials, with the potential for tuning by elastic deformation or integrated microfluidics. © 2012 American Institute of Physics. [doi:10.1063/1.3665180]

Terahertz (THz) or T-ray radiation is attracting much attention in recent years with the development of biomedical imaging, security screening, manufacturing quality control, and sensors.^{1–3} Terahertz applications are further augmented by the progress made in the field of metamaterials, since natural materials only exhibit weak electric and magnetic responses at terahertz frequencies.⁴ Metamaterials, unlike natural materials, can be artificially tailored to exhibit strong resonant behavior at terahertz frequencies.

Since the first demonstration of metamaterials for microwave frequencies,⁵ the majority of demonstrated metamaterials have been fabricated on rigid substrates. However, there is demand for flexible metamaterials that can be wrapped around objects for cloaking applications⁶ or attached to curved surfaces to serve as strain sensors.³ In addressing this need, flexible split-ring structures on polyimide⁶ and parylene⁷ have recently been reported, as well as crosses embedded in benzocyclobutene.⁸

In this work, a fishnet metamaterial structure is realized at terahertz frequencies by using flexible material as a substrate. The fishnet structure is generally comprised of two metal layers, which is well served by planar processing. Moreover, in the terahertz frequency regime, fishnet unit cell dimensions are in the micro-scale and compatible with standard semiconductor fabrication techniques. Unlike the planar arrays of split-ring resonators, fishnets are capable of exhibiting negative permittivity and negative permeability simultaneously, achieving the negative index of refraction required for a number of applications such as perfect lenses.⁹ Fishnet structures also allow the realization of polarization insensitive designs.¹⁰

While polyimide⁶ and parylene⁷ are suitable as flexible substrates, in this work, we have chosen the elastomeric silicone polymer—polydimethylsiloxane (PDMS), which is a low cost highly elastic material that is already widely used in microfluidics and nanofabrication.^{11–13} Also, the low surface

energy of PDMS allows conformal adhesion to curved surfaces.

As a silicone polymer, PDMS is known to have stable dielectric properties and low transmission loss.¹⁴ This behavior is verified in the terahertz regime using a free-space coupled terahertz time-domain spectroscopy (THz-TDS) system, equipped with a photoconductive antenna for T-ray generation and electro-optical detection. The pumping laser was a mode-locked Ti:sapphire laser with a central wavelength of 800 nm, a pulse duration of <100 fs, and a repetition rate of 80 MHz. The system generated pulsed T-ray radiation spanning 0.05–2.8 THz, with a maximum dynamic range of 30 dB. The collimated beam diameter was approximately 10 mm.

The PDMS samples under test were 375 and 960 μm thick sheets. Reference measurements were conducted at room temperature. The index of refraction and the absorption coefficient for both thicknesses were determined, with similar characteristics obtained. The refractive index and absorption coefficient for the 960 μm thick PDMS sheet in the terahertz region are shown in Figs. 1(a) and 1(b), respectively. The absorption coefficient of 20 cm^{-1} at 1.0 THz compares well with that of 30 cm^{-1} for polyimide.⁶ Using these results, the dielectric constant and loss tangent of PDMS were estimated as 2.35 and 0.02–0.04, respectively, across 0.2–2.5 THz band. This relatively low absorption of PDMS is significant to a reduction of loss in metamaterials.¹⁵

The unit cell of the proposed fishnet structure^{10,16} is shown in Fig. 2. The structure consists of patterned metallic layers embedded in PDMS. This fishnet is independent of polarization of the incident wave due to its symmetric square structure. Using these dielectric properties, fishnet structures were designed using Ansoft HFSS software (based on the full-wave finite element method). The structure is simulated as both periodic and infinite in the x - y plane. The incident wave is normal to the plane of the structure, and the electric and the magnetic fields are parallel to y -axis and x -axis, respectively.

The simulated performance of the designed fishnet is presented as supplemental material (Fig. S1).¹⁷ The fishnet

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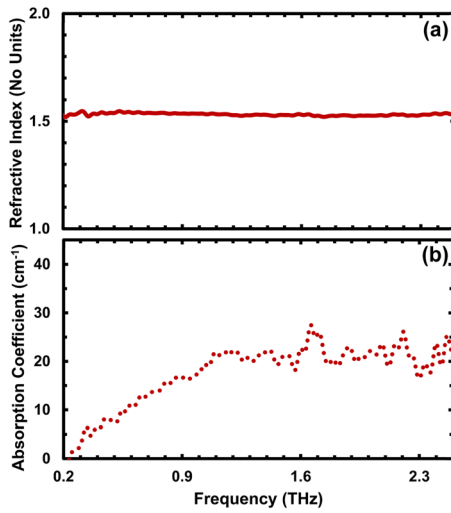


FIG. 1. (Color online) Properties of a $960\ \mu\text{m}$ thick PDMS sheet measured in the terahertz region: (a) index of refraction and (b) absorption coefficient.

exhibits a magnetic resonance at 2.1 THz due to antiparallel currents induced in the first and second layers of the structure by the magnetic field passing between the metal layers. The currents form an inductive-capacitive LC loop within each unit cell, with the spacer between the layers acting as a capacitor and metal slabs acting as inductors.¹⁸

The effective permittivity and permeability of the fishnet, presented in Fig. 3, were extracted from the simulation results.¹⁹ The sample transmission and reflection coefficients were de-embedded (based on Fig. 2) to compensate for the phase shift in the outer PDMS layers. The structure clearly shows a negative permittivity below 1.7 THz [Fig. 3(a)] and a negative permeability at 2.1 THz [Fig. 3(b)]. These engineered negative properties are clear evidence of the metamaterial effect of the sub-wavelength resonator features. However, in our realized structure, these electric and magnetic properties are not found at the same frequency as would be required for a negative refractive index metamaterial. Such a structure could be achieved by optimizing the unit cell to account for the plasma frequency of the wire grid.

The behavior of the fishnet structure is strongly dependent on the direction of flow of its surface currents. The surface current in the top and bottom metal layers of the fishnet at 2.1 THz is presented in Figs. 4(a) and 4(b), respectively. This shows that the current flows in opposite directions, as is expected at the frequency of the magnetic resonance and, hence, the negative permeability.¹⁹ The current distribution at electric resonance is presented in the supplemental mate-

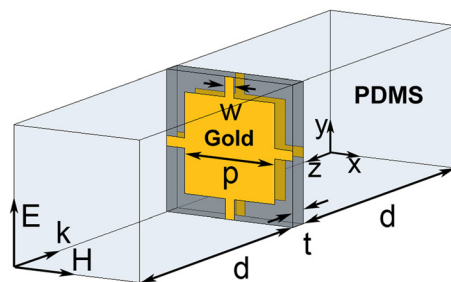


FIG. 2. (Color online) Fishnet unit cell with the following parameters: cell dimensions $70 \times 70 \times 510\ \mu\text{m}^3$, $p = 50\ \mu\text{m}$, $w = 5\ \mu\text{m}$, $t = 10\ \mu\text{m}$, and $d = 250\ \mu\text{m}$ for both outer encapsulating PDMS layers.

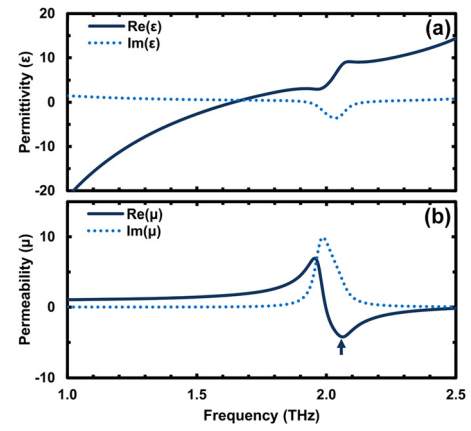


FIG. 3. (Color online) Effective permittivity and permeability of the double layer fishnet in PDMS are shown in (a) and (b), respectively.

rial as Fig. S2.¹⁷ A video depicting the evolution of surface currents to illustrate the physical model of the terahertz fishnet is also presented as supplemental material (Video S1).¹⁷

The fishnet structures are fabricated for experimental validation exploiting standard microfabrication techniques that are adapted to flexible, elastomeric device fabrication.²⁰ The fishnets have a total of 5 layers, with alternating layers of PDMS (3 layers) and patterned metal (2 layers). PDMS is spin coated on to a silicon wafer²¹ to obtain a thickness of $250\ \mu\text{m}$. Metal layers are deposited on the PDMS coated wafer using electron beam evaporation at room temperature. Alternating layers of chromium (20 nm) and gold (200 nm) are deposited with three layers of chromium encapsulating two layers of gold. The alternating layers are to minimize thin film stress and also to have chromium as the outer layers to improve adhesion to PDMS, resulting in a $460\ \text{nm}$ thick metal layer. The metal layers are patterned using standard photolithography techniques. Full details on the fabrication and patterning processes are provided as supplemental material. A thin layer of PDMS ($10\ \mu\text{m}$) is spin-coated on the first metal fishnet layer to serve as the dielectric separating the two fishnet layers. Following the curing of this layer, the multi-layer metallization and etching process are repeated to define the second fishnet layer, with an alignment process during photolithography. The fabrication process is completed by spin coating and curing a $250\ \mu\text{m}$ thick PDMS layer. The resulting 5-layered symmetric structure is peeled off from the supporting silicon substrate to realize a flexible fishnet metamaterial [Fig. 5(a)].

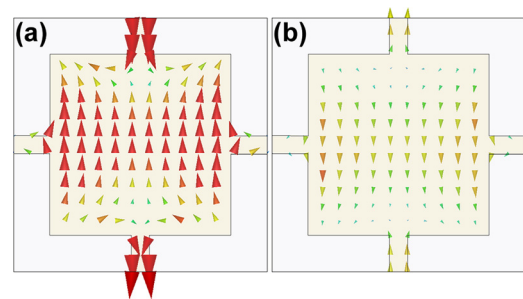


FIG. 4. (Color online) Distribution of the surface current of the (a) top and (b) bottom metal layers of the fishnet at the frequency of negative permeability ($\sim 2.1\ \text{THz}$). The opposite direction of current flow at magnetic resonance can be observed.

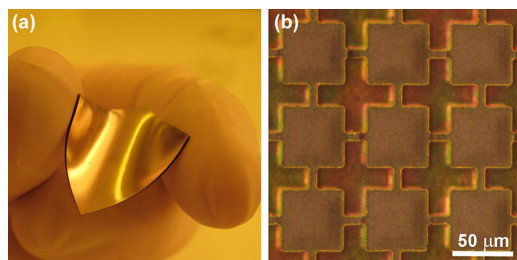


FIG. 5. (Color online) (a) Photograph of a section of the microfabricated elastomeric fishnet structure. (b) Optical micrograph showing 9 fishnet unit cells; the void between the metallization appears as a cross, where a slight misalignment between the two metal layers can be observed. The dimensions of the fabricated structure are as presented in Fig. 2.

The elastomeric property of PDMS, which this work aims to capitalize on, poses a challenge in the alignment of layers during the patterning of the second fishnet layer with respect to the first. The contact lithography process occurs with a wedge error correction process, meaning one edge of the wafer comes into contact with the photolithography mask first, before the rest gradually comes in contact. This typically results in a 2–5 μm misalignment error in the multilayer elastomer samples. Figure 5(b) shows a fabricated fishnet structure with 3 μm misalignment in both x and y directions. The influence of this misalignment on the expected terahertz spectra is determined by HFSS modeling with the results presented¹⁷ in Fig. S3. The misalignment causes a slight splitting of both the stop band and also the ensuing pass band. Despite this slight splitting, the structure shows good tolerance to misalignment, in which the magnitude and the position of the transmission band remain almost the same.

Figure 6 compares the simulated and measured results for transmission through the fishnet structure. Good agreement between theoretical and experimental results is observed. Resonant dips are evident at 2.0 THz and 2.1 THz as predicted by the simulations of a slightly misaligned fishnet. Splitting in the high transmission area after resonance is also evident in both the experimental measurements and theoretical predictions. The lowered transmission below 1.65 THz is caused by the negative permittivity achieved by the metamaterial. The simulated results provide a best fit to the experimental results for a loss tangent of 0.02, validating the low loss characteristics of the elastomeric PDMS substrates. The weak oscillations observed in the measurement are caused by Fabry-Pérot reflections (discussed in supplemental material)¹⁷ and do not affect the performance of the fishnet.

In conclusion, we have demonstrated the fabrication and characterization of a fishnet metamaterial operating in the terahertz frequency range using the flexible elastomer PDMS for all dielectric layers. A strong magnetic resonance is observed. The fishnet embedded in thick PDMS outer layers shows high transmission values in the pass bands highlighting the low propagation loss of the PDMS material. The structure exhibits a high tolerance to layer misalignment, maintaining the approximate position and strength of the resonances with only slight splitting of the resonances observed as a result of layer misalignment. Our future work will explore the utilization of the microfluidic capabilities of PDMS to enable fluid infiltration for tuning and sensing

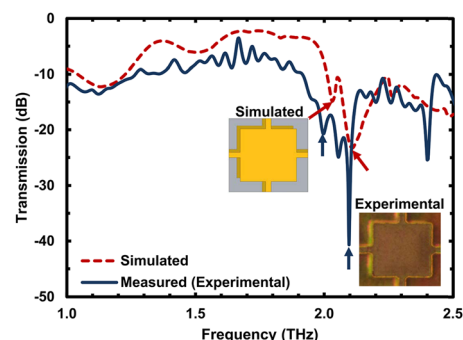


FIG. 6. (Color online) Simulated and measured terahertz response of PDMS-based fishnet structures. Good agreement can be observed in transmission intensity and resonant dip position, including the expected stop band splitting due to the 3 μm misalignment.

applications. We will also explore the conformal and adhesive properties of PDMS to use this realized terahertz fishnet as an *in situ* remotely interrogated sensing platform.

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