Regular Articles

Extremely low material loss and dispersion flattened TOPAS based circular porous fiber for long distance terahertz wave transmission

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\textbf{A B S T R A C T}

In this paper, we present a porous-core circular photonic crystal fiber (PC-CPCF) with ultra-low material loss for efficient terahertz wave transmission. The full vector finite element method with an ideally matched layer boundary condition is used to characterize the wave guiding properties of the proposed fiber. At an operating frequency of 1 THz, simulated results exhibit an extremely low effective material loss of 0.043 cm\textsuperscript{-1}, higher core power fraction of 47\% and ultra-flattened dispersion variation of 0.09 ps/THz/cm. The effects of important design properties such as single mode operation, confinement loss and effective area of the fiber are investigated in the terahertz regime. Moreover, the proposed fiber can be fabricated using the capillary stacking or sol-gel technique and be useful for long distance transmission of terahertz waves.

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1. Introduction

For the last few years, researchers have been concentrating their attention on the terahertz band for its numerous technological applications in the fields of sensing [1], biotechnology [2], imaging [3–5], spectroscopy [6] and communication [7] etc. At present, long distance transmission of terahertz waves is limited due to higher material absorption loss. Still now, most of the terahertz transmission depends on free space for its wave propagation [8]. Dependency on free space has some undesirable problems such as sensitive alignment, path loss, uncertain absorption loss and difficult integration with other components. To overcome these problems, various kinds of guided transmission media have been previously reported [9–13].

At the early stages of development of guided transmission media, researchers showed that metallic wires [9] and metal-coated dielectric tubes [10] can be used as a transmission medium but the dilemma of using metal waveguides was due to high bending loss, low coupling efficiency and unbalanced guidance in a complex atmosphere [11,12]. Later, plastic subwavelength fibers [13] came into existence for their comparatively lower losses. However, most of the field propagates outside the waveguide core, thus resulting in strong coupling to the environment. For improvement, Nagel et al. [14] reported a fiber with the addition of a subwavelength hole within a solid core, which increases the guided field in the air hole, hence reducing the absorption losses. However, the loss due to the material was still high.

A research breakthrough occurred when polymer materials were used instead of metals allowing a much lower absorption loss. The polymer materials PMMA [15], Teflon [16], TOPAS [17], Zeonex [18] etc can be used as the initial choices for THz waveguidance. However, PMMA and Teflon were not considered in the design of our waveguide because of their higher losses than TOPAS and Zeonex [19]. Note that, TOPAS was used as the bulk material in our designed PCF. The motivation behind using TOPAS rather than other materials includes, (i) lower material absorption loss, (ii) low density, (iii) glass transition temperature much higher than PMMA [20], (iv) multi-antibody biosensing [21], (v) high transparency, (vi) humidity insensitive [22], (vii) excellent biocompatibility, (viii) constant refractive index n = 1.53 in the frequency range of 0.1–1.5 THz [17], (ix) negligibly hygroscopic [23], which results in lower terahertz absorption and is advantageous for manufacturing terahertz waveguides. Zeonex on the other side is an ultra high
purity optical grade polymer widely used in optical applications where refractive index stability over a high temperature and humidity range is crucial. Please note that, TOPAS and Zeonex foam can be drawn together into a single mode step-index fiber [24].

To reduce the material absorption loss further, polystyrene foam [25] was introduced but it required much larger dimensions. Hollow core Bragg fibers [26–27] were also introduced but disregarded due to their unwanted narrow band properties. Photonic crystal fiber (PCF) [17] is a micro-structured optical waveguide with finite number of air holes in the cladding. Note that a PCF with solid cores has been introduced but it is found that the material absorption loss of solid core is too high [17] and almost equal to the bulk absorption loss of the used material. Recently, to improve field confinement and reduce effective material loss (EML) further, studies have used a porous core surrounded by air cladding [29].

To date researchers have proposed several polymer waveguides, of which porous core PCF’s [29–35] gained much attention. The distinction between porous core PCF and conventional PCF is that the solid core of the conventional PCF is replaced by number of smaller air holes in the porous core PCF. Based on the concept of porous core, both porous core and hollow core honeycomb band-gap fiber have been proposed [36] and after numerical and experimental investigation, studies have found that porous core fiber has wider bandgap, lower total propagation loss and is easier to manufacture than hollow core fiber.

For characterization of terahertz porous fibers Atakaramians et al. [28] developed a technique by exploiting a micro-machined photoconductive probe-tip. They showed a loss less than 0.08 cm−1 within the frequency range of 0.2–0.3 THz with minimal loss of 0.03 cm−1 at a frequency of 0.24 THz. Mechanically down-doped low loss directional couplers were also proposed [43,44] for broadband terahertz applications. The down-doping was achieved by introducing micro-structured air holes in the core.

In 2013, Kaijage et al. [29] proposed a porous core octagonal photonic crystal fiber with TOPAS as the base material for terahertz wave guidance. They realized an effective material loss of 0.076 cm−1 but did not perform analysis for dispersion and core power fraction properties of the fiber. Later, Ranaqul et al. [30] reported a porous core fiber having a rotating hexagonal core structure and a hexagonal cladding structure. Later Rana et al. [31] proposed a porous fiber having octagonal structure in both core and cladding. They were able to reduce the EML further to 0.058 cm−1 although omitted to characterize the dispersion properties. However, Hasan et al. [32] proposed a fiber having a circular structure in the core and an octagonal structure in the cladding. They demonstrated a comparatively lower EML of 0.056 cm−1 without exploring the single-mode limits of the fiber. Furthermore, Ranaqul et al. [33] proposed a circular structure in both core and cladding. They showed comparatively lower EML of 0.053 cm−1 with dispersion flattened properties. In 2015, H. Bao et al. [19] proposed a dielectric tube waveguide with absorptive cladding for broadband applications. Ranaqul et al. [34] proposed a low-loss diamond core porous fiber having EML of 0.07 cm−1, but the loss is actually higher. Later, Hasan et al. [35] proposed a slotted core kagome lattice terahertz fiber and showed an EML of 0.05 cm−1, however the problem is that the loss is still higher and the fabrication of slotted core is difficult. Recently, Saiful et al. [37] proposed another waveguide with octagonal structure in the cladding and a rotated hexagonal structure in the core. They showed comparatively lower EML and flatten dispersion profile when 49.1% useful light propagates through the core.

For further improvement, a TOPAS based porous fiber having hexagonal array of air-holes in the core and circular array of air-holes in the cladding structure is presented in this paper. The EML of the proposed fiber is 0.043 cm−1, which is about 78.5% less than the bulk absorption material loss of TOPAS and almost half of the useful power goes through the core air holes. As the propagation of light through our designed fiber is based on modified total internal reflection (MTIR), the effects of external environment can totally be neglected. Thus it is expected that the fiber can efficiently be applied to the transmission of broadband terahertz waves.

2. Model design

Fig. 1 depicts the proposed fiber with an enlarged version of the core. In the designed PC-CPCF, five rings of air holes for circular cladding and three rings of air holes for hexagonal core structure are considered.

The spacing between two adjacent air holes in the cladding on two adjacent rings is denoted by a. The spacing between air holes lying on the same ring is A1, which is related to A by A1 = 0.765 A. For the core, the spacing between two air-holes on two adjacent rings and that on the same ring is A. The diameter of air holes in cladding region is denoted by d and df. Two air holes in the first ring of the cladding are kept smaller than the other air holes with diameter df. The presence of these smaller air holes in the first ring of the cladding made it possible to increase the core porosity that hence reduces the EML. Note that simulating this type of structure of the fiber does not introduce computational complexity. During simulation, with the variation of core diameter Dcore = 2(A – d/2), the air holes of diameter d were varied automatically but the air holes of diameter df were varied manually. The air filling fraction (AFF) df/A was kept fixed at 0.76 throughout the numerical analysis for a good confinement factor. The value of AFF should not be increased further due to fabrication difficulties. In the meantime, the AFF in the core diameter is intentionally varied and mostly determined by the core porosity. Porosity is defined as the ratio of the air hole area to the total cross-section area of the core.

3. Simulation procedure and results

The full vector finite element method (FEM) based software COMSOL, version 4.3b is used for simulating the characteristics of the fiber. A perfectly matched layer (PML) boundary condition is used to absorb the incident radiation without producing reflections, which is about 10% of the total fiber radius. The finalized geometry has 159 domains, 636 boundaries, and 636 vertices. The full structure contains 31,980 elements and 4515 boundary elements. The power flow distribution of the proposed fiber at different core porosities is shown in Fig. 2. It is observed from Fig. 2 that light is well confined inside the core of the fiber.

First, we have to be ensuring that the single mode condition of the proposed fiber is not affected with the modification of core diameter and frequency. Considering this fact, the single mode properties were analysed carefully by a parameter called V–parameter. Normalized frequency or V–parameter can be calculated by [27].

\[
V = \frac{2\pi rf}{c} \sqrt{n_{cl}^2 - n_{cl}^2} \leq 2.405,
\]

where r is defined as the core radius, c is the speed of light in vacuum, ncl and ncl are considered to be the refractive indices of core and cladding respectively. The core refractive index ncl is considered to be effective refractive index (ncl) because of the porous core. Theoretically, we can assume ncl to be unity because of the large number of air holes in the cladding [29–35], but practically it must be slightly greater than unity as cladding is a combination of air and material. The characteristics of the V–parameter are calculated for different values of ncl. Thus, satisfying Eq. (1), it is observed from Figs. 3 and 4 that, as the ncl increases with core
Then we focus on absorption loss or effective material loss of the proposed fiber. The EML of a fiber can be calculated by [27],

\[
\alpha_{\text{eff}} = \sqrt{\epsilon_0 \mu_0} \left( \frac{\int_{\text{mat}} n_{\text{mat}} |E|^2 n_{\text{mat}} \, dA}{\int_{\text{all}} S_z \, dA} \right)
\]

where \(\epsilon_0\) and \(\mu_0\) are considered to be the relative permittivity and permeability in vacuum respectively, \(n_{\text{mat}}\) is the refractive index of TOPAS, \(a_{\text{mat}}\) is the bulk material absorption loss, \(E\) is the modal electric field and \(S_z\) is the \(z\) component of the pointing vector \(S_z = -\frac{1}{2}(E \times H')z\), where \(E\) and \(H\) are the electric and magnetic fields respectively. Fig. 5 depicts the characteristics of EML as a function of core diameter with different core porosities. It is clearly observable that, for the same porosity values EML is almost constant when the core diameter changes. The EML basically depends upon the amount of material used in the core. It is also observed from Fig. 5 that as the porosity decreases the EML increases. As the porosity decreases, the size of air holes in the core decreases which in turn increases the amount of material and thus increase EML. It is clearly depicted that at a core diameter of 300 \(\mu\text{m}\) and frequency of 1 THz, minimal EML of 0.043 cm\(^{-1}\) is obtained which is less than the previously proposed in Refs. [29–35].
The amount of useful power propagating through the fiber core can be calculated by [38],

\[
\eta' = \frac{\int_{s_{core}} S_{dA}}{\int_{s_{total}} S_{dA}}
\]

where \( \eta' \) represents mode power fraction and \( X \) represents the area of interest. To design a standard PCF, it is necessary to pass most of the useful power through the core air holes. Higher \( D_{core} \) increases the core power fraction but with the increase of EML, on the contrary EML decreases with the decrease of \( D_{core} \), but this also decrease the core power fraction. These are contradictory conditions and need to select an optimum condition for getting higher core power fraction and lower EML. At different core porosities, the characteristics of core power fraction as a function of core diameter is shown in Fig. 6, where it can be observed that the amount of core power increases with the increase of core diameter. It is further observed from the same figure that, at 81% core porosity, \( f = 1 \) THz frequency and \( D_{core} = 300 \mu m \) shows 47% of the total power propagating through the core air holes which is sufficient for terahertz wave guidance.

Now, it is important to note that, in TOPAS, the bulk material absorption loss is not constant over the frequency range of 0.65–1.3 THz rather it increases linearly with frequency [39]. So, according to the empirical formula [39]: \( \alpha (\nu) = \nu^2 + 0.63\nu - 0.13 \) [dB/cm], it is experimentally demonstrated through Fig. 7 that the bulk material absorption loss depends on frequency. This matter is carefully observed when calculating the frequency response loss characteristics of the fiber. From Fig. 8 one can deduce that as the frequency increases from 1 THz, the EML increases and core power fraction decreases. The electromagnetic frequency is proportional to the EML and hence as the frequency increases the EML also increases. Furthermore, from Fig. 8, it is evident that the EML is minimum and core power fraction is higher at an operating frequency of \( f = 1 \) THz with 81% core porosities.

Another important parameter to be considered for PCF design is confinement loss. It depends upon the core porosity and the number of air holes used in cladding. It can be calculated by taking the imaginary part of the complex refractive index. The confinement loss can be calculated by [18],

\[
LC = 8.686 \left( \frac{2nf}{c} \right) \text{Im}(n_{eff}) \text{ dB/m}
\]

where \( f \) is the frequency of the guiding light, \( c \) is speed of light in vacuum and \( \text{Im}(n_{eff}) \) yields the imaginary part of the refractive index. The confinement loss as a function of frequency is shown in Fig. 9, from where it is observed that as the frequency increases, the confinement loss scaled down. In our designed fiber, at \( f = 1 \) THz, \( D_{core} = 300 \mu m \) and 81% porosity, a confinement loss of the order of \( 10^{-2.5} \text{ cm}^{-1} \) is obtained which is negligible compared to the calculated EML.

Next we discuss the dispersive properties of the proposed fiber. As stated in Ref. [39] that the refractive index of TOPAS is constant in between the frequency range of 0.1–1.5 THz, its material dispersion can totally be neglected in this band. So only the waveguide dispersion is analysed in our proposed fiber. The dispersion parameter \( \beta_2 \) can be calculated by [18],

\[
\beta_2 = \frac{2}{c} \frac{dn_{eff}}{d\omega} + \frac{\omega}{c} \frac{d^2n_{eff}}{d\omega^2}.
\]
The calculated dispersion as a function of frequency is shown in Fig. 10. It can be observed from Fig. 10 that the flatness of dispersion is achieved from 1–1.3 THz where $\beta_2 < 1.23 \text{ ps/THz/cm}$ and $\beta_2 > 1.05 \text{ ps/THz/cm}$, so the variation in dispersion is less than 0.09 ps/THz/cm.

The effective area ($A_{\text{eff}}$) of the proposed fiber is also addressed and can be calculated by [42],

$$ A_{\text{eff}} = \frac{\int |I(r)|^2 dr}{\int |F^2 (r)| dr} \quad (6) $$

where $|I(r)| = |E_0|^2$ is defined as the transverse electric field intensity distribution in the cross section of the fiber. The $A_{\text{eff}}$ as a function of frequency is shown in Fig. 11, from where it is observed that as the frequency increases from 0.9 THz, the $A_{\text{eff}}$ decreases. The reason being more light is confined in the core for $f > 1$ THz. It is also observed that at operating parameters, the calculated $A_{\text{eff}}$ is very much comparable to those in Refs. [29, 42].

Finally, it is necessary to discuss the fabrication possibilities for the fiber. Stack and drilling, capillary stacking and sol-gel techniques are the most commonly used techniques for PCF fabrication. As our proposed fiber comprised of circular air holes, capillary stacking [40] and sol-gel [41] techniques can be the best choice to fabricate our proposed PCF where the dimension of the designed PCF can be adjusted freely.

4. Conclusion

A comparatively simple single mode TOPAS based PC-PCF with ultra-low material loss, higher core power fraction and ultra-flattened dispersion is proposed in this paper. The significance of our proposed PCF is extremely low EML and simplicity in design. Ultra–low material loss and flattened dispersion potentially have significant application in long distance transmission of terahertz signals. On the other hand, higher core power fraction potentially have wide application in terahertz wave guidance. Therefore, if the proposed fiber is utilized properly, it can open the door for convenient, efficient, long distance and flexible transmission of terahertz signals.

References


Fig. 10. Frequency dependent dispersion at $D_{\text{core}} = 300$ μm and porosity = 81%.

Fig. 11. Effective mode area as a function of frequency at $D_{\text{core}} = 300$ μm.


